

## COMPARISON OF THE METHODOLOGIES FOR THE DETERMINATION OF THE BELT TENSIONS AND THE REQUIRED DRIVE POWER OF THE BELT CONVEYORS

**Hristo Sheiretov**

University of Mining and Geology "St. Ivan Rilski", 1700 Sofia; sheiretov@abv.bg

**ABSTRACT.** Four methodologies are discussed: short and precise methodology of the Design, Science and Research Institute for Industrial Transport (Promtransniiproekt), Russia; short and precise methodology according to the German calculation standard for belt conveyors DIN 22101.

The calculations are accomplished using the four methodologies for a concretely solved example - a stationary all-purpose belt conveyor with assigned layout profile, type and characteristic of the transported material, capacity, belt width and belt velocity, linear mass of the material, the belt and the idlers. In the calculations an equal coefficient of motional resistance and an equal coefficient of friction between the belt and the drive pulley are assumed. The belt tensions at start-up and at steady state working and the required drive power are determined.

The following conclusions are drawn: 1. Approximately equal values are obtained for the required drive power; 2. Smaller values are obtained for the belt tensions in the precise methodology in comparison with the short methodology. 3. Higher values are obtained for the belt tensions in the DIN methodology in comparison with the Promtransniiproekt methodology. The reason is the difference in the methods for determination. 4. It should be noticed that the coefficient of motional resistance in the Promtransniiproekt methodology is recommended to be taken greater in comparison with the DIN methodology, which will lead to the increase of the belt tensions.

**Keywords:** belt tensions, drive power, methodology

### СРАВНЯВАНЕ НА МЕТОДИКИТЕ ЗА ОПРЕДЕЛЯНЕ НА СИЛИТЕ НА ОПЪН В ЛЕНТАТА И МОЩНОСТТА НА ЗАДВИЖВАНЕТО НА ЛЕНТОВИТЕ ТРАНСПОРТЪОРИ

**Христо Шейретов**

Минно-геоложки университет "Св. Иван Рилски", 1700 София

**РЕЗЮМЕ.** Разгледани са четири методики: приблизителна и уточнена методика на проектантския и научно-изследователски институт за промишлен транспорт (Промтрансниiproekt), Русия; приблизителна и уточнена и методика по немския стандарт за изчисляване на лентови транспортъори DIN 22101.

Направени са изчисления по четирите методики за конкретно решаван пример - стационарен общопрмишлен транспортъор със зададени профил на трасето, вид и характеристика на транспортирания материал, производителност, ширина и скорост на лентата, линейни маси на материала, лентата и ролковите опори. При изчисленията е приет еднакъв коефициент на съпротивление при движението на лентата и еднакъв коефициент на триене между лентата и задвижващия барабан. Определени са силите на опън в лентата при пусков и установен режим и необходимата мощност на задвижването.

Направени са следните изводи: 1. За необходимата мощност на задвижването се получават близки по значение стойности; 2. За силите на опън в лентата при уточнената методика се получават по-малки стойности в сравнение с приблизителната методика; 3. За силите на опън в лентата по двете уточнени методики при методиката на DIN се получават по-големи стойности. Причина за това е разликата в начина им на определяне; 4. Трябва да се отбележи, че по методиката на Промтрансниiproekt се препоръчва коефициентът на съпротивление при движение да се приема по-голям в сравнение с методиката на DIN, което ще доведе до увеличаването на силите на опън.

**Ключови думи:** сили на опън в лентата, мощност на задвижването, методика

### Introduction

There are different methodologies for the calculation and the design of the belt conveyors - the American standards ISO and CEMA, the German standard DIN, Russian methodologies, etc. Because of the differences in the methods for the determination of some parameters it will be useful to have a comparative evaluation of the calculation results using these methodologies.

The present research is a continuation of a previous research, in which the calculation results of the material cross section area and the capacity of the belt conveyor using three methodologies are compared (Journal of Mining and Geological Sciences, 2018).

The calculations in the present paper are accomplished using the following methodologies: the methodologies of the

Design, Science and Research Institute for Industrial Transport Promtransniiproekt, Russia - short and precise methodology (Posobie po proektirovaniyu konveyernogo transporta, 1988); the methodologies according to the German standard for belt conveyor design DIN 22101 - short and precise methodology (Dunlop conveyor belt design and calculation, Phoenix conveyor belt design fundamentals, 2004).

The aim of the present research is to calculate the belt tensions at start-up and at steady state working and the required drive power using the four methodologies and to compare the results. A concrete example is solved for a conveyor with a given layout profile, type and characteristic of the transported material, capacity, belt width and belt velocity, linear masses of the belt, the material and the idlers. In the calculations an equal coefficient of motional (primary) resistance and an equal friction coefficient between the belt and the drive pulley are assigned.

### Determination of the belt tensions and the required drive power using the different methodologies

#### Input data for the design

The calculations in the present research are accomplished for a stationary belt conveyor with the following parameters: length of the horizontal projection of the conveyor  $L_r = 200$  m; lifting height  $H = 24$  m; transported material limestone with density  $\rho = 1,5$  t/m<sup>3</sup>; belt width  $B = 800$  mm; belt velocity  $v = 1.6$  m/s.

#### Determination of the geometric parameters of the layout profile of the conveyor (according to Fig.1)

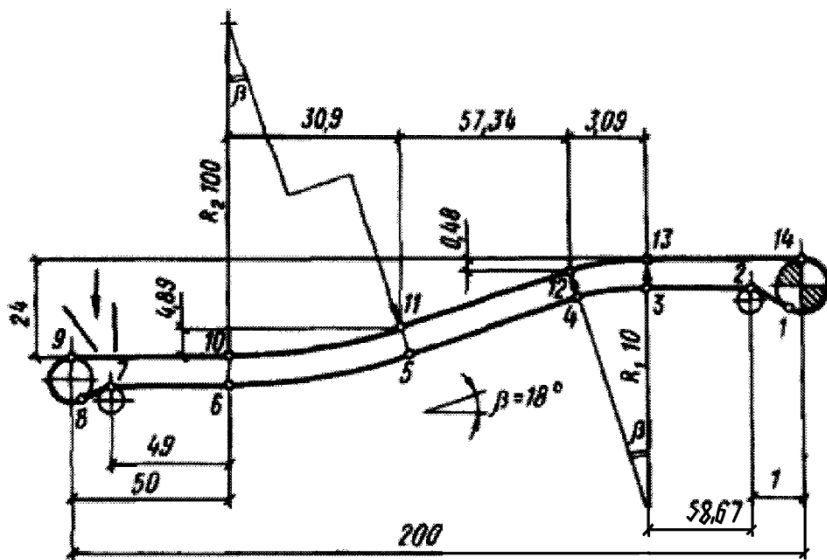


Fig.1. Scheme of the layout profile of the conveyor

Initially it is assumed: angle of inclination of the conveyor  $\beta = 18^\circ$  (the maximum permissible angle for the transportation of limestone); radius of the concave curve  $R_2 = 100$  m (the minimum permissible radius at belt width  $B = 800$  mm); radius of the convex curve  $R_1 = 10$  m (the minimum permissible radius at  $B = 800$  mm and an angle of inclination of the side rollers  $\lambda = 30^\circ$ ); length of the horizontal section  $l_{9-10} = 50$  m; length of the horizontal projections of the sections  $l_{1-2} = l_{7-8} = 1$  m.

The lengths of the horizontal projections  $l_{i-j}$  and the lifting heights  $h_{i-j}$  of the other sections are:

$$l_{10-11} = l_{5-6} = R_2 \cdot \sin\beta = 30.9 \text{ m} \quad (1)$$

$$h_{10-11} = h_{5-6} = R_2 - R_2 \cdot \cos\beta = 4.89 \text{ m} \quad (2)$$

$$l_{12-13} = l_{3-4} = R_1 \cdot \sin\beta = 3.09 \text{ m} \quad (3)$$

$$h_{12-13} = h_{3-4} = R_1 - R_1 \cdot \cos\beta = 0.48 \text{ m} \quad (4)$$

$$h_{11-12} = h_{4-5} = H - h_{10-11} - h_{12-13} = 18.63 \text{ m} \quad (5)$$

$$l_{11-12} = l_{4-5} = \frac{h_{11-12}}{\tan\beta} = 57.34 \text{ m} \quad (6)$$

$$l_{13-14} = L_r - l_{10-11} - l_{11-12} - l_{12-13} = 58.67 \text{ m} \quad (7)$$

$$l_{6-7} = l_{9-10} - l_{7-8} = 49 \text{ m} \quad (8)$$

$$l_{2-3} = l_{13-14} - l_{1-2} = 57.67 \text{ m} \quad (9)$$

The length of the conveyor is:

$$L = l_{9-10} + \frac{2 \cdot \pi \cdot \beta \cdot R_2}{360} \cdot \frac{l_{11-12}}{\cos\beta} + \frac{2 \cdot \pi \cdot \beta \cdot R_1}{360} + l_{13-14} = 203.5 \text{ m} \quad (10)$$

#### Short methodology of Promtransniiproekt

Required peripheral forces of the drive pulley at start-up and steady state working

$$P = k_\delta \cdot k'_\delta \cdot L_r \cdot w \cdot (q_M + q'_p + q''_p + 2 \cdot q_n) + q_M \cdot H = 24370 \text{ N} \quad (11)$$

$$P_n = k_\delta \cdot k'_\delta \cdot L_r \cdot w_n \cdot (q_M + q'_p + q''_p + 2 \cdot q_n) + q_M \cdot H = 26780 \text{ N}, \quad (12)$$

where:  $k_\delta$  - coefficient of the additional resistances from belt bending (it is chosen from Table 1 according to the conveyor length  $L$ ; at  $L \approx 200$  m  $k_\delta = 1.45$ );

$k'_\delta$  - correction coefficient (at horizontal conveyors and at inclined conveyors with length  $L < 100$  m  $k'_\delta = 1$ ; at inclined conveyors with length  $L \geq 100$  m  $k'_\delta$  is chosen from Table 2; at  $L \approx 200$  m and  $n = 5$   $k'_\delta = 1.15$ );

$w, w_n$  - coefficients of motional resistance during the belt movement at start-up and at steady state movement (at normal

conditions of exploitation they are assumed to be  $w = 0.020$  and  $w_n = 0.026$ );  
 $q_m$  - linear gravity force of the material ( $q_m = 681$  N/m at conveyor capacity  $Q = 400$  t/h and belt velocity  $v = 1,6$  m/s);  
 $q_p^1, q_p^2$  [dN/m] - linear gravity forces of the rotating parts of the carry and return idlers (they are assumed to be  $q_p^1 = 179$  N/m and  $q_p^2 = 64$  N/m at belt width  $B = 800$  mm, density of the material  $\rho = 1.5$  t/m<sup>3</sup> and idler pitches  $l_p^1 = 1$  m и  $l_p^2 = 2.2$  m);  
 $q_n$  [dN/m] - linear gravity force of the belt (it is assumed to be  $q_n = 140$  dN/m at  $B = 800$  mm).

Table 1. Coefficient of additional resistances  $k_\delta$

L [m]	10	20	30	50	60	80	100
$k_\delta$	4.5	3.2	2.6	2.2	2.1	1.91	1.75

L [m]	120	140	160	180	<b>200</b>	250	300
$k_\delta$	1.7	1.6	1.55	1.5	<b>1.45</b>	1.38	1.32

L [m]	350	400	500	700	800	1000
$k_\delta$	1.28	1.24	1.19	1.12	1.095	1.087

Table 2. Correction coefficient  $k_\delta'$

L [m]	100	150	<b>200</b>	300	500	$\geq 800$
$n = 3 - 5$	1.04	1.13	<b>1.15</b>	1.3	1.42	1.53
$n = 6 - 10$	1.21	1.31	1.42	1.54	1.66	1.81

L - length of the conveyor; n - number of belt bending over the drive and non-drive pulleys and the convex sections of the conveyor. For the solved example (Fig.1)  $n = 5$ .

**Belt tensions in the points of entering and leaving of the drive pulley at start-up and steady state working**

$$S_{en} = S_{14} = \frac{e^{\mu\alpha} \cdot P}{(e^{\mu\alpha} - 1)} = 33740 \text{ N} \quad (13)$$

$$S_{en}^n = S_{14}^n = \frac{e^{\mu\alpha} \cdot P_n}{(e^{\mu\alpha} - 1)} = 37080 \text{ N} \quad (14)$$

$$S_{u3n} = S_1 = S_{en} - P = 9370 \text{ N} \quad (15)$$

$$S_{u3n}^n = S_1^n = S_{en}^n - P_n = 10300 \text{ N} \quad (16)$$

where:  $\mu$  - coefficient of friction between the belt and the drive pulley (it is assumed  $\mu = 0.35$  at rubber lagged pulley and dry surfaces);  
 $\alpha$  - wrap angle of the belt ( $\alpha = 210^\circ = 3.66$  rad).

**Required power on the shaft of the drive pulley**

$$N_6 = \frac{P \cdot v}{1000} = 39 \text{ kW} \quad (17)$$

**Precise methodology of Promtransniiproekt**

**Belt tensions**

The belt tensions are determined using the method of going round of the contour. The resistances of the sections  $W_{i,j}$  are added consecutively to the belt tension in the point of leaving from the drive pulley  $S_1 = S_{u3n}$  and the remaining

tensions are obtained. For the solved example for the start-up period it is obtained (according to the scheme of Fig.1):

$$S_1^n = S_{u3n}^n \quad (18)$$

$$S_2^n = S_1^n + W_{1-2}^n = S_1^n + 0,02 \cdot S_1^n \quad (19)$$

$$S_3^n = S_2^n + W_{2-3}^n = S_2^n + (q_n + q_p^2) \cdot w_n \cdot l_{2-3} \quad (20)$$

$$S_4^n = S_3^n + W_{3-4}^n = S_3^n + [S_3^n + (q_n + q_p^2) \cdot R_1] \cdot \beta \cdot w_n \quad (21)$$

$$S_5^n = S_4^n + W_{4-5}^n = S_4^n + (q_n + q_p^2) \cdot w_n \cdot l_{4-5} - q_n \cdot h_{4-5} \quad (22)$$

$$S_6^n = S_5^n + W_{5-6}^n = S_5^n + (q_n + q_p^2) \cdot w_n \cdot l_{5-6} - q_n \cdot h_{5-6} \quad (23)$$

$$S_7^n = S_6^n + W_{6-7}^n = S_6^n + (q_n + q_p^2) \cdot w_n \cdot l_{6-7} \quad (24)$$

$$S_8^n = S_7^n + W_{7-8}^n = S_7^n + 0,02 \cdot S_7^n \quad (25)$$

$$S_9^n = S_8^n + W_{8-9}^n = S_8^n + 0,04 \cdot S_8^n \quad (26)$$

$$S_{10}^n = S_9^n + W_{9-10}^n = S_9^n + (q_m + q_n + q_p^1) \cdot w_n \cdot l_{9-10} \quad (27)$$

$$S_{11}^n = S_{10}^n + W_{10-11}^n = S_{10}^n + (q_m + q_n + q_p^1) \cdot w_n \cdot l_{10-11} + (q_m + q_n) \cdot h_{10-11} \quad (28)$$

$$S_{12}^n = S_{11}^n + W_{11-12}^n = S_{11}^n + (q_m + q_n + q_p^1) \cdot w_n \cdot l_{11-12} \quad (29)$$

$$S_{13}^n = S_{12}^n + W_{12-13}^n = S_{12}^n + [S_{12}^n + (q_m + q_n + q_p^1) \cdot R_1] \cdot \beta \cdot w_n \quad (30)$$

$$S_{14}^n = S_{en}^n = S_{13}^n + W_{13-14}^n = S_{13}^n + (q_m + q_n + q_p^1) \cdot w_n \cdot l_{13-14} = 1,097 \cdot S_1^n + 22231 \quad (31)$$

On the other hand:

$$S_{14}^n = S_1^n \cdot e^{\mu\alpha} = 3.61 \cdot S_1^n \quad (32)$$

When the equations (31) and (32) are solved together, the tension  $S_{1n}$  is obtained:

$$1.097 \cdot S_1^n + 22231 = 3.61 \cdot S_1^n \quad (33)$$

$$S_1^n = 8870 \text{ N} \quad (34)$$

Using the formulae (19)-(31) the remaining tensions are obtained. The tensions at steady state of working are obtained by analogy, but the coefficient of motional resistance is taken  $w = 0.020$  instead of  $w_n = 0.026$ . The results from the calculations of the belt tensions at start-up and at steady state working are given in Table 3.

Table 3. The results from the calculations of the belt tensions at start-up and at steady state working

Formula for calculation ( $w_n=0.026$ )	Belt tensions [N]	
	Start-up $w_n=0.026$	Steady state $w = 0.020$
$S_1^n = 8870$	$S_1^n = 8870$	$S_1 = S_{u3n}=8250$
$S_2^n = 1.02 \cdot S_1^n$	$S_2^n = 9050$	$S_2 = 8420$
$S_3^n = 1.02 \cdot S_1^n + 306$	$S_3^n = 9350$	$S_3 = 8660$
$S_4^n = 1.036 \cdot S_1^n + 358$	$S_4^n = 9370$	$S_4 = 8650$
$S_5^n = 1.036 \cdot S_1^n - 2048$	$S_5^n = 7070$	$S_5 = 6280$
$S_6^n = 1.036 \cdot S_1^n - 2567$	$S_6^n = 6550$	$S_6 = 5720$
$S_7^n = 1.036 \cdot S_1^n - 2307$	$S_7^n = 6810$	$S_7 = 5920$
$S_8^n = 1.056 \cdot S_1^n - 2354$	$S_8^n = 6940$	$S_8 = 6030$
$S_9^n = 1.098 \cdot S_1^n - 2448$	$S_9^n = 7210$	$S_9 = 6270$
$S_{10}^n = 1.98 \cdot S_1^n + 1148$	$S_{10}^n = 8510$	$S_{10} = 7270$
$S_{11}^n = 1.098 \cdot S_1^n + 3662$	$S_{11}^n = 13320$	$S_{11} = 11890$
$S_{12}^n = 1.098 \cdot S_1^n + 20457$	$S_{12}^n = 30110$	$S_{12} = 28340$
$S_{13}^n = 1.11 \cdot S_1^n + 20706$	$S_{13}^n = 30430$	$S_{13} = 28580$
$S_{14}^n = 1.11 \cdot S_1^n + 22231$	$S_{14}^n = 31960$	$S_{14} = S_{en} = 29750$

**Required peripheral force on the drive pulley**

$$P = \frac{S_{en} - S_{u3n}}{\eta_6} = 23120 \text{ N} \quad (35)$$

where:  $\eta_6$  - coefficient of efficiency of the drive pulley (it is determined by formula (36))

$$\eta_6 = \frac{1}{1 + w_6 \cdot \left( 2 \cdot \frac{e^{\mu \cdot \alpha}}{e^{\mu \cdot \alpha} - 1} - 1 \right)} = 0.93 \quad (36)$$

where:  $w_6$  - coefficient of resistance of the drive pulley taking an account of the belt bending (it is assumed to be  $w_6=0.04$ ).

**Required power on the shaft of the drive pulley**

$$N_6 = \frac{P \cdot v}{1000} = 37 \text{ kW} \quad (37)$$

**Short methodology according to the standard DIN 22101**

**Required drive power**

$$P_T = P_1 + P_2 + P_3 = 35.8 \text{ kW} \quad (38)$$

where:  $P_1$  [kW] - required power for the belt and the material moving on the rollers (it is determined by formula (39));

$P_2$  [kW] - required power for the material lifting (it is determined by formula (40));

$P_3$  [kW] - sum of the required additional powers for the trippers, side boards and unloading ploughs (when there are no trippers boards and ploughs  $P_3=0$ );

$$P_1 = \frac{c_B \cdot v + Q_m}{c_L \cdot k_f} = 9.7 \text{ kW} \quad (39)$$

$$P_2 = \frac{H \cdot Q_m}{367} = 26.1 \text{ kW} \quad (40)$$

where:  $c_B$  - coefficient depending on the belt width and the density of the transported material (it is determined by Table 4; at  $B = 800 \text{ mm}$  and  $\rho = 1.5 \text{ t/m}^3$  it is assumed  $c_B = 126$ );

$c_L$  - coefficient depending on the conveyor length (it is determined by Table 5; at  $L = 203,5 \text{ m}$  after interpolation it is assumed  $c_L = 62$ );

$k_f$  - coefficient depending on the working conditions (it is determined by Table 6; at medium (normal) working conditions  $k_f = 1$ ).

Table 4. Coefficient  $c_B$  depending on the belt width

$\rho$ [t/m <sup>3</sup> ]	Belt width B [mm]					
	650	800	1000	1200	1400	1600
< 1	81	108	133	194	227	291
1-2	92	126	187	277	320	468
> 2	103	144	241	360	414	644

$\rho$  - density of the material

Table 5. Coefficient  $c_L$  depending on the conveyor length

L [m]	10	20	32	50	80	100	150	200
$c_L$	417	286	222	167	119	103	77	63

100	150	200	250	300	500	800	1000	2000
103	77	63	53	47	31	20	17	9

Table 6. Coefficient  $k_f$  depending on the working conditions of the conveyor

Working conditions	$k_f$
Light Good belt centering, small belt velocity	1.17
Medium (normal, standard)	1
Heavy Dusty atmosphere, low temperatures, overloading, high belt velocity	0.87 – 0.74

**Precise methodology according to the standard DIN 22101**

**Belt tensions at steady state working**

According to the scheme of Fig.1 the correspondence of the belt tensions is:  $T_2$  to  $S_1$ ,  $T_3$  to  $S_8$ ,  $T_4$  to  $S_9$  и  $T_1$  to  $S_{14}$ .

$$T_2 = F_U \cdot c_2 = 8910 \text{ N} \quad (41)$$

$$T_3 = T_2 + F_u - F_{Stu} = 6330 \text{ N} \quad (42)$$

$$T_4 = T_3; \quad T_1 = T_4 + F_N + F_o + F_{Sto} = 32070 \text{ N} \quad (43)$$

where:  $F_U$  - total peripheral force on the drive pulley (it is determined by formula (44));

$c_2$  - drive factor for the determination of the belt tension in point of leaving from the drive pulley (it is determined by formula (45));

$F_o$ ,  $F_u$  - primary resistances in the carry and the return run (from the belt and material movement, rotation of the rollers, bending of the belt, strike of the belt to the rollers, inner friction of material etc. (they are determined by the formulae (46) and (47));

$F_{Stu}$ ,  $F_{Sto}$  - gradient resistances in the carry and the run side (they are determined by the formulae (48) and (49));  
 $F_N$  - total secondary resistance (from the bending of the belt around the pulleys, friction in the pulley bearings, resistances in the loading and cleaning devices, etc. (it is determined by the formula (50)).

$$F_U = F_H + F_N + F_{St} = 23170 \text{ N} \quad (44)$$

$$c_2 = \frac{1}{e^{\mu_A \alpha} - 1} = 0.3846 \quad (45)$$

$$F_o = f.L.g.[m'_{Ro} + (m'_G + m'_L).cos\delta] = 3910 \text{ N} \quad (46)$$

$$F_u = f.L.g.(m'_{Ru} + m'_G).cos\delta = 790 \text{ N} \quad (47)$$

$$F_{Sto} = H.g.(m'_G + m'_L) = 19710 \text{ N} \quad (48)$$

$$F_{Stu} = H.g.m'_G = 3370 \text{ N} \quad (49)$$

$$F_N = (C - 1).F_H = 2120 \text{ N} \quad (50)$$

where:  $f$  - coefficient of motional (primary) resistance (it is assumed  $f = w = 0.02$ );  
 $m'_{Ro}$ ,  $m'_{Ru}$  - linear masses of the rotating parts of the idlers in the carry and the return run (they are assumed according to the previously chosen  $q'_p = 179 \text{ N/m}$  and  $q''_p = 64 \text{ N/m}$  -  $m'_{Ro} = 18.3 \text{ kg/m}$  and  $m'_{Ru} = 6.5 \text{ kg/m}$ );  
 $m'_G$ ,  $m'_L$  - linear masses of the belt and the material (they are assumed according to the previously chosen  $q_n = 140 \text{ N/m}$  and  $q_m = 681 \text{ N/m}$  -  $m'_G = 14.3 \text{ kg/m}$  and  $m'_L = 69.4 \text{ kg/m}$ );  
 $\delta$  - angle of inclination of the conveyor ( $\delta = \beta = 18^\circ$ );  
 $C$  - coefficient of secondary resistance (corresponds to the coefficient  $k_\delta$ ; it is assumed  $C = k_\delta = 1.45$  from Table 1);  
 $F_H$  - total primary resistance (it is determined by the formula (51));  
 $F_{St}$  - total gradient resistance (it is determined by the formula (52)).

$$F_H = f.L.g.[m'_{Ro} + m'_{Ru} + (2.m'_G + m'_L).cos\delta] = 4710 \text{ N} \quad (51)$$

$$F_{St} = H.g.m'_L = 16340 \text{ N} \quad (52)$$

#### Belt tensions at start-up

$$T_{A2} = F_A.c_{2A} = 10590 \text{ N} \quad (53)$$

$$T_{A3} = T_{A2} + F_u - F_{Stu} + F_{au} = 10020 \text{ N} \quad (54)$$

$$T_{A4} = T_{A3} = 10020 \text{ N} \quad (55)$$

$$T_{A1} = T_{A4} + F_N + F_o + F_{Sto} + F_{ao} = 45750 \text{ N} \quad (56)$$

where:  $c_{2A}$  - drive factor at start-up (it is determined by the formula (57));  
 $F_{au}$ ,  $F_{ao}$  - acceleration forces in the carry and return run (they are determined by the formulae (58) and (59));

$$c_{2A} = \frac{1}{e^{\mu_A \alpha} - 1} = 0.3009 \quad (57)$$

$$F_{ao} = L.a_A.(0.9.m'_{Ro} + m'_G + m'_L) = 9990 \text{ N} \quad (58)$$

$$F_{au} = L.a_A.(0.9.m'_{Ru} + m'_G) = 2010 \text{ N} \quad (59)$$

where:  $\mu_A$  - coefficient of friction between the belt and the pulley at start-up (it is determined by the formula (60));  
 $a_A$  - acceleration of the conveyor at start-up (it is determined by the formula (61));

$$\mu_A = \mu + 0.05 = 0.4 \quad (60)$$

$$a_A = \frac{F_A - F_U}{L.(0.9.m'_{Ro} + 0.9.m'_{Ru} + 2.m'_G + m'_L)} = 0.49 \text{ m/s}^2 \quad (61)$$

where:  $F_A$  - peripheral force on the drive pulley at start-up (it is determined by the formula (62)).

$$F_A = k_A.F_U = (1.2 \div 1.5).F_U = 1.3.F_U = 35200 \text{ N} \quad (62)$$

#### Correction of the belt tensions at the steady state working according to the kind of the tension device

A condition is used that the belt tensions in the point, where the tension weight is put (in this case on the return pulley), at start-up and steady state working are equal. This means that  $T_{A4} = T_4$ . Then for the belt tensions at steady state working after the correction with the value of  $\Delta T = T_{A4} - T_4$  it is finally obtained:

$$T_{A4} = T_4; \quad \Delta T = T_{A4} - T_4 = 3690 \text{ N} \quad (63)$$

$$T_1 = T_1 + \Delta T = 35760 \text{ N} \quad (64)$$

$$T_2 = T_2 + \Delta T = 12600 \text{ N} \quad (65)$$

$$T_3 = T_4 = T_3 + \Delta T = 10020 \text{ N} \quad (66)$$

#### Required drive power

$$P_T = \frac{F_U.v}{1000} = 37 \text{ kW} \quad (67)$$

#### Conclusions

The results of the calculations are generalised in Table 7.

Table 7. Comparative results of the calculations of the belt tensions and the required drive power

Methodology	1	2	3	4
$T_1 (S_{14}, S_{en})$ [N]	33740	29750	-	35760
$T_2 (S_1, S_{uzn})$ [N]	9370	8250	-	12600
$T_3 (S_8)$ [N]	-	6030	-	10020
$T_4 (S_9)$ [N]	-	6270	-	10020
$T_{A1} (S_{14}^n)$ [N]	37080	31960	-	45750
$T_{A2} (S_1^n)$ [N]	10300	8870	-	10590
$T_{A3} (S_8^n)$ [N]	-	6940	-	10020
$T_{A4} (S_9^n)$ [N]	-	7210	-	10020
$P_T (N_6)$ [kW]	39	37	35,8	37

1 - Promtransniiproekt short; 2 - Promtransniiproekt precise; 3 - DIN 22101 short; 4 - DIN 22101 precise.

The following conclusions can be drawn from the calculations using the four discussed methodologies:

1. Approximately equal values are obtained for the required drive power  $P_T$  ( $N_6$ ). The highest is the value obtained by methodology 1 and the smallest - by methodology 3.

2. a Smaller values are obtained for the belt tensions according to the precise methodology (methodology 2) in comparison with the short methodology (methodology 1).

3. Higher values are obtained for the belt tensions using the precise methodologies (2 and 4) according to methodology 4 in comparison with methodology 2. The reason is the difference in the methods for their determination. In methodology 2 the belt tensions at start-up are determined in the same way as at steady state working, but a higher coefficient of motional resistance is assumed. In methodology 4 the acceleration forces at start-up are considered.

4. Higher values are obtained for the belt tensions at steady state working using the precise methodologies in methodology 4. The reason is the correction (increase) of the tensions in accordance with the condition, that in the point

where the tension weight is put the tensions at start-up and steady state working are equal.

5. The calculations are accomplished at equal coefficients of motional (primary) resistance  $f(w)$ . It should be noticed, that in methodologies 1 and 2 it is recommended to take higher coefficients of motional in comparison with methodologies 3 and 4. This will lead to the increase of the belt tensions, determined by methodologies 1 and 2.

## References

- Conveyor Handbook. Conveyor belt technique. Design and calculation.* 2009. Fenner Dunlop.
- Oreshkin, V. L., V. K. Dyachkov, O. V. Zelenskiy. 1988. *Posobie po proektirovaniyu konveyernogo transporta. Lentochnyie konveyeryi.* Stroyizdat, Moscow (in Russian).
- Phoenix conveyor belt design fundamentals. DIN 22101.* 2004. Hamburg.